

Possibility of Charge Density Wave Instability in the Barium Tungsten Bronze  $\text{Ba}_{0.15}\text{WO}_3$ 

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Received July 8, 1993\*

The electronic band structure of the  $\text{Ba}_{0.15}\text{WO}_3$  phase was calculated by employing the extended Hückel tight-binding method, and the nature of the partially filled bands was analyzed.  $\text{Ba}_{0.15}\text{WO}_3$  has partially filled bands of one-dimensional (1D) as well as three-dimensional (3D) character. Consequently,  $\text{Ba}_{0.15}\text{WO}_3$  may exhibit a charge density wave (CDW) instability due to the 1D bands but may remain metallic, even after a predicted CDW, because of the 3D band.

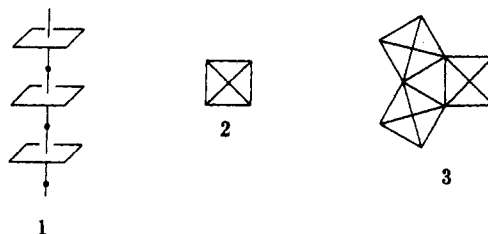
## Introduction

Barium tungsten bronze  $\text{Ba}_x\text{WO}_3$  ( $0 < x < 0.13$ ) was first prepared and found to be metallic by Conroy and Yokokawa.<sup>1</sup> Soon  $\text{Ba}_x\text{WO}_3$  ( $x = 0.13$ ) was reported to become a superconductor at 1.9 K by Sweedler et al.<sup>2</sup> A systematic study of  $\text{Ba}_x\text{WO}_3$  ( $0.01 < x < 0.33$ ) phases was carried by Ekström and Tilley,<sup>3</sup> who showed that the Ba–W–O system consists of several bronze types, i.e., the tetragonal tungsten bronze (TTB), the orthorhombic intergrowth tungsten bronze (ITB), and  $\text{Ba}_{0.15}\text{WO}_3$ . The study of Ekström and Tilley suggests<sup>3</sup> that the  $\text{Ba}_{0.13}\text{WO}_3$  sample prepared by Sweedler et al.<sup>2</sup> is biphasic, containing orthorhombic ITB materials and a larger amount of either the TTB phase or the  $\text{Ba}_{0.15}\text{WO}_3$  phase. From the observations that the TTB phase of the Ba–W–O system is closely related to the tin TTB phase,  $\text{Sn}_x\text{WO}_3$ ,<sup>4</sup> which does not become superconducting at least down to 1.3 K,<sup>5</sup> and that only the smaller fraction of Sweedler et al.'s sample ( $\sim 35\%$ ) became superconducting, Ekström and Tilley suggested<sup>3</sup> that the superconducting component of Sweedler et al.'s sample<sup>2</sup> was most likely the orthorhombic ITB part. However, there is no compelling reason why the  $\text{Ba}_{0.15}\text{WO}_3$  phase cannot be a superconducting component. The X-ray crystal structure of  $\text{Ba}_{0.15}\text{WO}_3$  was determined by Michel et al.,<sup>6</sup> who showed that the structure of  $\text{Ba}_{0.15}\text{WO}_3$  is similar to those of  $\text{KCuM}_3\text{O}_9$  ( $M = \text{Nb}, \text{Ta}$ ).<sup>7</sup> The electrical resistivity and thermoelectric power measurements for compressed pellets of powder samples and magnetic susceptibility measurements of powder samples show<sup>8</sup> that  $\text{Ba}_{0.15}\text{WO}_3$  is a metal with electron-type carriers. All these physical measurements were carried out down to  $\sim 100$  K, so that it is unknown whether or not  $\text{Ba}_{0.15}\text{WO}_3$  remains metallic below  $\sim 100$  K. So far no electronic band structure study has been reported for these barium tungsten bronze systems. In the present work, we calculate the electronic band structure of  $\text{Ba}_{0.15}\text{WO}_3$  on the basis of the extended Hückel tight binding (EHTB) method<sup>9</sup> and analyze the nature of its partially filled bands to

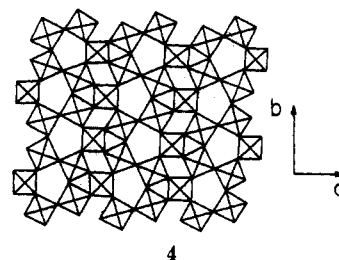
examine the anisotropy of the metallic properties. The atomic orbital parameters of our EHTB calculations were taken from our previous study.<sup>10</sup>

## Crystal Structure

For our discussion of the electronic band structure of  $\text{Ba}_{0.15}\text{WO}_3$ , it is necessary to describe the essential elements of its crystal structure.  $\text{Ba}_{0.15}\text{WO}_3$  is made up of  $\text{WO}_6$  octahedra by sharing their corners. A corner-sharing of  $\text{WO}_6$  octahedra leads to a  $\text{WO}_5$  chain 1, which can be represented by a top-projection view



2. The  $\text{W}_3\text{O}_{12}$  chain 3 is obtained when three  $\text{WO}_5$  chains share their corners. Alternatively, the  $\text{W}_3\text{O}_{12}$  chain may be considered as constructed from  $\text{W}_3\text{O}_{15}$  cluster units (i.e., the repeat units of the  $\text{W}_3\text{O}_{12}$  chain capped with three oxygen atoms, which are also represented by the projection view 3) by sharing their three axial oxygen atoms. As shown in 4, the  $\text{W}_3\text{O}_{12}$  chains share their corners to form the three dimensional (3D) lattice of  $\text{Ba}_{0.15}\text{WO}_3$ , which has trigonal, tetragonal and pentagonal channels parallel to the crystallographic c-axis. The  $\text{Ba}^{2+}$  ions reside in the pentagonal tunnels of 4.



In the crystal structure, the  $\text{W}_3\text{O}_{12}$  chains are distorted as shown in 5. The  $\text{W}(2)\text{O}_6$  and  $\text{W}(2')\text{O}_6$  octahedra have the same geometry, being related by the mirror plane of symmetry that

\* Abstract published in *Advance ACS Abstracts*, April 1, 1994.

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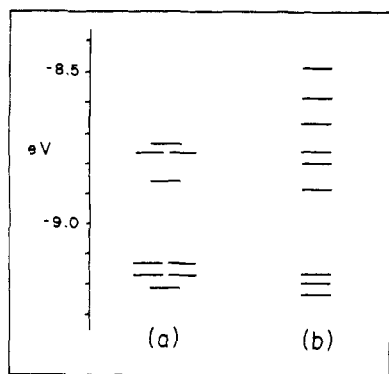
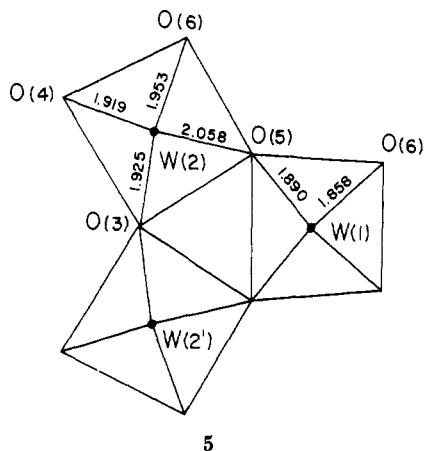


Figure 1. Comparison of the  $t_{2g}$ -block levels calculated for (a) the ideal  $W_3O_{15}$  cluster and (b) the real  $W_3O_{15}$  cluster.

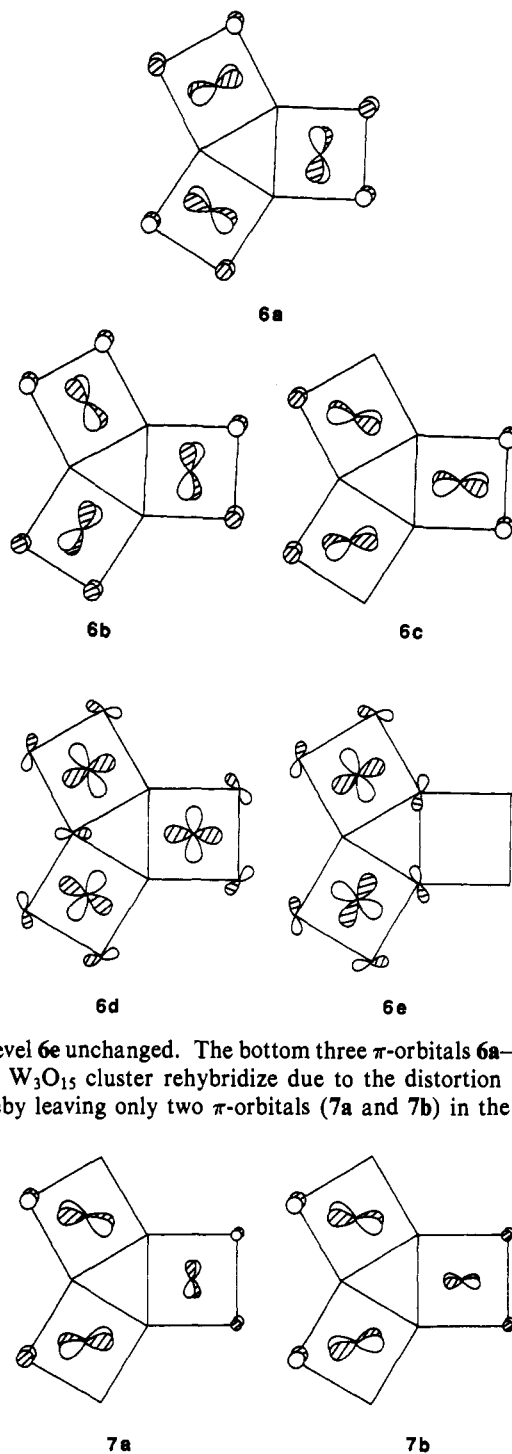


bisects the  $W(1)O_6$  octahedron. The  $W(1)-O(6)$  bonds (1.86 Å) are short compared with other  $W-O$  bonds, and the  $O(5)-W(1)-O(6)$ ,  $O(6)-W(1)-O(6)$ ,  $O(3)-W(2)-O(5)$ , and  $O(5)-W(2)-O(6)$  angles are smaller than  $90^\circ$ . Apart from these, the  $WO_6$  octahedra are reasonably regular in shape. In particular, there is no strong  $W-O\cdots W$  bond length alternation (1.904, 1.931 Å) along the  $W_3O_{12}$  chain direction. In condensing the  $W_3O_{12}$  chains to form the 3D lattice 4, the  $W(1)O_6$  octahedra share the  $O(6)$  atoms with the  $W(2)O_6$  and  $W(2')O_6$  octahedra, while the  $W(2)O_6$  octahedra share the  $O(4)$  atoms with the  $W(2')O_6$  octahedra. These structural features play a crucial role in determining the nature of the bottom portion of the d-block bands, as discussed below.

#### Low-Lying $t_{2g}$ Levels of the $W_3O_{15}$ Cluster Unit

With the typical oxidation states of  $O^{2-}$  and  $Ba^{2+}$ , there are 0.3 electron per tungsten atom in the d-block bands of  $Ba_{0.15}WO_3$ , so that only the bottom portions of its  $t_{2g}$ -block bands are filled. Since the transport properties of a metal are primarily determined by its partially filled bands, we focus on the bottom portion of the  $t_{2g}$ -block bands. The characteristic building blocks of  $Ba_{0.15}WO_3$  are the  $W_3O_{12}$  chains. Since these chains are made up of the  $W_3O_{15}$  cluster units, we first examine the  $t_{2g}$ -block levels of the  $W_3O_{15}$  cluster.

Figure 1a shows the nine  $t_{2g}$ -block levels calculated for the ideal  $W_3O_{15}$  cluster. (Here the ideal  $W_3O_{15}$  cluster was constructed from regular  $WO_6$  octahedra of  $W-O = 1.93$  Å, which is the average of the  $W-O$  lengths in 5.) The bottom five levels of the ideal cluster are described by the orbitals 6a–e. Along the chain direction, the orbitals 6a–c make  $\pi$ -type interactions, and the orbitals 6d,e make  $\delta$ -type interactions. Figure 1b shows the nine  $t_{2g}$ -block levels calculated for the real  $W_3O_{15}$  cluster. Due to the distortion 3  $\rightarrow$  5, the real  $W_3O_{15}$  cluster has only three  $t_{2g}$ -levels as low in energy as the bottom five  $t_{2g}$ -levels of the ideal cluster. The most significant change of the distortion 3  $\rightarrow$  5 is the  $W(1)-O(6)$  bond shortening (see 5), which raises the level 6d and leaves



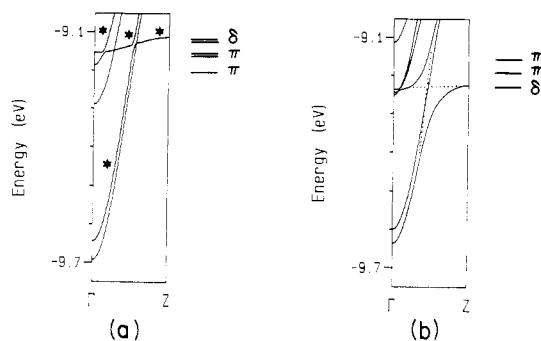
the level 6e unchanged. The bottom three  $\pi$ -orbitals 6a–c of the ideal  $W_3O_{15}$  cluster rehybridize due to the distortion 3  $\rightarrow$  5, thereby leaving only two  $\pi$ -orbitals (7a and 7b) in the energy

region of 6e. An important consequence of the distortion is that the orbital contribution of the  $W(1)$  atom is made much smaller in 7a,b than in 6a–c, thereby reducing the extent of antibonding in the shortened  $W(1)-O(6)$  bonds.

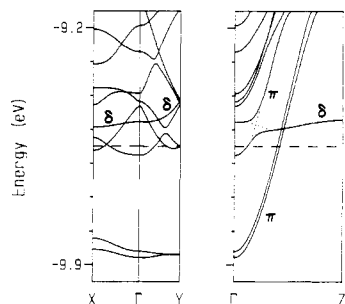
#### Electronic Band Structure

**$W_3O_{12}$  Chain.** The bottom portions of the  $t_{2g}$ -block bands calculated for the ideal  $W_3O_{12}$  chains are shown in Figure 2a, where the bands indicated by a star are doubly degenerate. For comparison, the bottom five  $t_{2g}$ -block levels of the ideal  $W_3O_{15}$  cluster are shown on the right-hand side of Figure 2a. The bands derived from the  $\pi$ -orbitals of the  $W_3O_{15}$  clusters are very dispersive, because the absence of  $W-O\cdots W$  bond alternation along the chain direction provides strong  $\pi$ -interactions (see 8 and 9).<sup>11,12</sup> The bands derived from the  $\delta$ -orbitals of the  $W_3O_{15}$

(11) Whangbo, M.-H.; Canadell, E. *Acc. Chem. Res.* 1989, 22, 375.



**Figure 2.** Comparison of the bottom portions of the  $t_{2g}$ -block bands calculated for (a) the ideal  $W_3O_{12}$  chain and (b) the real  $W_3O_{12}$  chain. The bands labeled by a star are doubly degenerate.  $\Gamma = 0$  and  $Z = c^*/2$ .



**Figure 3.** Bottom portion of the  $t_{2g}$ -block bands calculated for the  $WO_3$  lattice of the  $Ba_{0.15}WO_3$  phase. The dashed line represents the Fermi level.  $\Gamma = (0, 0, 0)$ ,  $X = (a^*/2, 0, 0)$ ,  $Y = (0, b^*/2, 0)$  and  $Z = (0, 0, c^*/2)$ .

clusters are nearly dispersionless because the bridging oxygen orbitals cannot mix with the d orbitals of adjacent W atoms (see **10**).<sup>11,12</sup> Because of the strong dispersion, the bottom of the lowest several  $\pi$ -bands lies well below the  $\delta$ -bands.

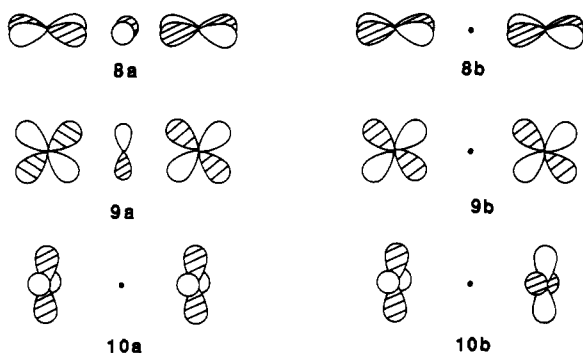
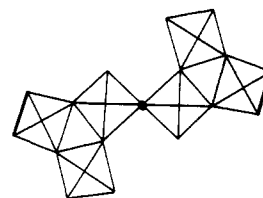


Figure 2b shows the bottom portion of the  $t_{2g}$ -block bands calculated for the real  $W_3O_{12}$  chain. The three energy levels on the right hand side of Figure 2b represent the bottom three  $t_{2g}$ -block levels of the real  $W_3O_{12}$  cluster. Analysis of the orbital character reveals that the bottom three bands of Figure 2b are essentially derived from the bottom three d-block levels of the real  $W_3O_{12}$  cluster, i.e., **6e**, **7a**, and **7b**. Of these three, one  $\pi$ -band and one  $\delta$ -band strongly mix and switch their orbital character on going from  $\Gamma$  to  $Z$ , as indicated by dotted lines in Figure 2b. The bottom of the two  $\pi$ -bands represent the lowest portion of the  $t_{2g}$ -block bands.

**$WO_3$  Lattice.** Figure 3 shows the bottom portion of the  $t_{2g}$ -block bands calculated for the  $WO_3$  lattice of  $Ba_{0.15}WO_3$ . In essence, the bottom three bands of the 3D lattice **4** (compare Figures 2b and 3,  $\Gamma \rightarrow Z$ ) are similar in nature to those of real  $W_3O_{12}$  chain (Figure 2b); namely, they consist of two  $\pi$  band and one  $\delta$  band. Since the repeat unit of  $Ba_{0.15}WO_3$  is  $(Ba_{0.15}WO_3)_6$ ,

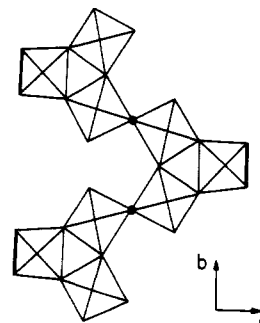
there are 1.8 electrons to put into these bands. The dashed line represents the Fermi level corresponding to this electron counting, and this level cuts the two partially filled bands that are strongly dispersive along the chain direction and nearly flat along the directions perpendicular to the chain direction. Another band cut by the Fermi level is dispersive along the three orthogonal directions. Consequently,  $Ba_{0.15}WO_3$  possesses partially filled bands of both one-dimensional (1D) and 3D character. The presence of the 1D bands suggests that  $Ba_{0.15}WO_3$  is likely to exhibit an electronic instability such as a charge density wave (CDW).<sup>12,13</sup> However, even if  $Ba_{0.15}WO_3$  undergoes a CDW transition, as predicted, it may still remain metallic due to the 3D band and may even become a superconductor at a low temperature.

**Orbital Character of the Partially Filled Bands.** It is of interest to examine why the bottom three bands of the 3D lattice **4** (Figure 3,  $\Gamma \rightarrow Z$ ) are similar in nature to those of the real  $W_3O_{12}$  chain (Figure 2b) and also why the two  $\pi$  bands of the 3D lattice are 1D in character. The condensation of the  $W_3O_{12}$  chains to form the 3D lattice **4** produces the W-O(6)-W and W-O(4)-W bridges in the directions perpendicular to the chain direction. The 3D lattice **4** can be built in terms of the unit cell **11a**, in which two



**11a**

$W_3O_{12}$  chains are condensed by a W-O(4)-W bridge. (For the purpose of clarity, the O(6)-O(6) side of each W(1)O<sub>6</sub> octahedron is represented by a thick line in **11a**). When this unit cell is repeated along the b-direction, one obtains a zigzag pattern of  $W_3O_{12}$  chains (**11b**) that are joined only by the W-O(4)-W



**11b**

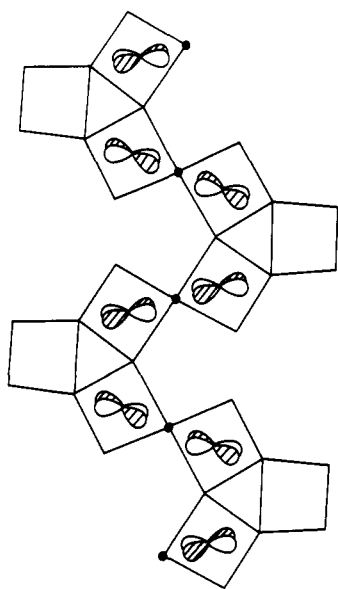
bridges. When the zigzag pattern **11b** is repeated along the a-direction, there occur only the W-O(6)-W bridges between them.

As illustrated in **8-10**, there occur three kinds of orbital interactions through a linear symmetric W-O-W bridge. In the  $\pi$  interactions, the p orbitals of the bridging ligand may or may not interact with the metals depending on the relative phases of the metal orbitals (**8a** vs **8b** and **9a** vs **9b**). As already pointed out, two condensed  $W_3O_{12}$  chains in a unit cell **11** of the 3D lattice make a W-O(4)-W bridge. Through this bridge, each of the orbitals **6e**, **7a**, and **7b** makes  $\pi$ -type in-phase and out-of-phase combinations. Therefore, there occur two sets of orbitals, the lower energy set with no orbital contribution from the O(4) atom, and the higher energy set with orbital contribution from

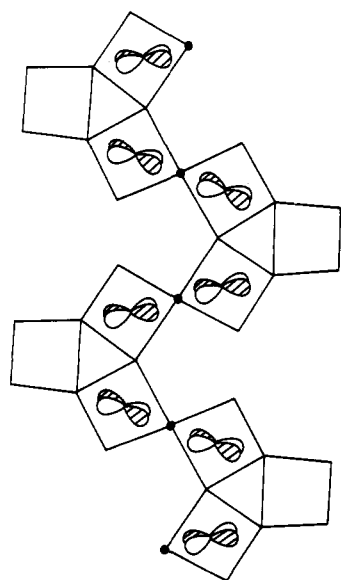
(13) Moret, R.; Pouget, J. P. in *Crystal Chemistry and Properties of Materials with Quasi-One-Dimensional Structures*; Rouxel, J., Ed.; Reidel: Dordrecht, The Netherlands, 1986; p 87.

the O(4) atom. It is the lower energy set that represents the three lowest energy bands of the 3D lattice.

In **7a** and **7b** the  $d_x$  orbitals of the W(2) and W(2') atoms are oriented such that they are nearly  $\delta$  orbitals with respect to the W(2)–O(6) and W(2')–O(6) bond axes. Consequently, any of the orbitals **7a** and **7b** cannot interact effectively through the W–O(6)–W bridges, so that all interactions between adjacent zigzag patterns **11b** vanish. This accounts for why the bottom two nearly-degenerate  $\pi$  bands exhibit only a weak dispersion along  $\Gamma \rightarrow X$ . We now consider why these two bands are flat along  $\Gamma \rightarrow Y$ . The zigzag pattern **11b** links the  $\text{W}_3\text{O}_{12}$  chains along the  $b$ -direction, which leads to the W–O(4)–W bridges between the  $\text{W}_3\text{O}_{12}$  chains. In **7a** and **7b**, the  $d_x$  orbitals of the W(2) and W(2') atoms are pseudo- $\delta$  orbitals along the  $b$ -direction. These  $d_x$  orbitals make  $\pi$ -type interactions through the W–O(4)–W bridges, so that the band levels with no p-orbital contributions of the bridging ligand O(4) atoms constitute the lowest-lying  $\pi$  bands. The nodal properties of the two lowest-lying  $\pi$  bands at  $\Gamma$  are shown in structure **12a,b**, and those at  $Y$  in structure **13a,b**. For the purpose of clarity, the  $d_x$  orbitals of

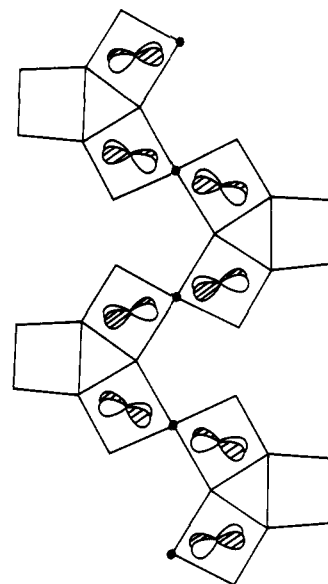


12a

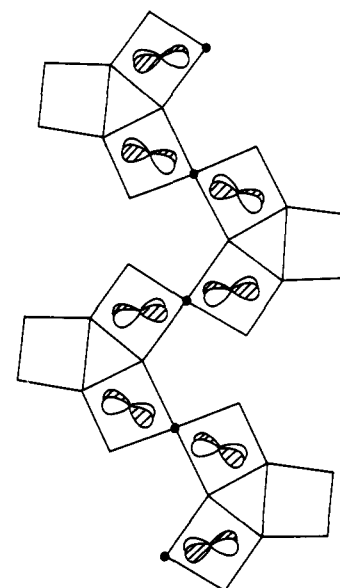


12b

W(1) are not shown in **12** and **13**. At  $\Gamma$ , the band orbital **12a**



13a



13b

is composed of the cluster orbitals **7a**, while the band orbital **12b** is composed of the cluster orbitals **7b**. At  $Y$ , however, each of the band orbitals **13a** and **13b** is constructed by combining the cluster orbitals **7a** and **7b**. (The levels **13a** and **13b** are degenerate as dictated by the glide plane of symmetry present in the zigzag pattern **11b**.) Clearly, in **12** and **13**, the  $d_x$  orbitals of the W(2) and W(2') atoms are pseudo- $\delta$  orbitals along the  $b$ -direction, so that all the levels of **12** and **13** are almost degenerate. This explains why the bottom two  $\pi$  bands are nearly degenerate and are flat along  $\Gamma \rightarrow Y$ .

In **6e** there is no d-orbital component on the W(1) atom, so that the **6e** do not interact through the W–O(6)–W bridges thereby leading to a flat band in the  $a$ -direction. Though not shown, the  $d_x$  orbitals of the W(2) and W(2') atoms of **6e** make  $\pi$ -type interactions through the W–O(4)–W bridges, so that the  $\delta$  band resulting from the cluster orbitals **6e** are dispersive along  $\Gamma \rightarrow Y$  (Figure 3). It should also be noted from Figure 3 that the partially filled band of 3D character in Figure 3 has  $\pi$  character. This band undergoes an avoided crossing with the  $\delta$  band along  $\Gamma \rightarrow Z$  and is dispersive in the directions perpendicular to the chain direction. This band is derived from a  $\text{W}_3\text{O}_{15}$  cluster orbital in which the  $d_x$  orbitals of the W(2) and W(2') atoms make  $\pi$  interactions through the W(2)–O(6) and W(2')–O(6) bonds, so

that it becomes dispersive along the directions perpendicular to the chain direction.

#### Concluding Remarks

Our calculations show that the  $\text{Ba}_{0.15}\text{WO}_3$  has both 1D and 3D bands. Due to the 1D bands,  $\text{Ba}_{0.15}\text{WO}_3$  may exhibit a CDW instability. If  $\text{Ba}_{0.15}\text{WO}_3$  undergoes a CDW transition, as predicted, it may still remain metallic due to the 3D band and may even become a superconductor at a low temperature. It is

highly desirable to carry out resistivity and X-ray diffraction measurements of single crystal samples of  $\text{Ba}_{0.15}\text{WO}_3$ .

**Acknowledgment.** This work was supported by the U.S. Department of Energy, Office of Basic Sciences, Division of Materials Sciences, under Grant DE-FG05-86ER45259, by NATO, under Grant CRG 910129 from the Scientific Affairs Division, and by Centre National de la Recherche Scientifique, France.